

# LCF Properties Investigation of Sn-3.5Ag-0.75Cu Solder Paste

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Keywords: Sn-3.5Ag-0.75Cu, solder paste, low-cycle fatigue, viscoplasticity

# Abstract.

This study is focused on research in tension-compression fatigue and uniaxial ratcheting. Strain controlled fatigue tests were done under constant strain amplitude loading considering a constant strain rate on a specially designed specimen. The influence of the mean stress and the stress amplitude on uniaxial ratcheting has been studied for three load frequencies. Results are consistent with the stress-strain behaviour observed under monotonic loading. Aim of this and previous investigations is to obtain experimental data of Sn-3.5Ag-0.75Cu solder paste for calibration of a viscoplastic material model for future finite element analysis and to propose appropriate fatigue damage model for subsequent computational fatigue analysis. First results gained by a non-unified constitutive model are also presented.

# Introduction

Tin based materials show strongly rate dependent stress-strain behaviour. Most of the studies which investigate the lead-free solder paste mechanical properties are mainly focused on ratedependent and thermal-dependent plasticity in monotonic loading [1] or secondary creep properties [2]. Uniaxial low-cycle fatigue was investigated for example by Ohguchi et al [3], but only stabilized hysteresis loops were published. The transient behavior seems to be out of scope for most of scientific studies. There are only few published works emphasized on accumulation of plastic strains due to non-zero mean stress (ratcheting), for example [4], [5].

This study follows the contributions, which were focused on measurement of mechanical properties in monotonic tension, monotonic torsion and creep [6] and low cycle fatigue in torsion of a lead-free solder paste [7].

# **Experiment description**

First, LCF tension-compression fatigue tests were performed for the constant strain rate of  $0.015 \text{ mm} \cdot \text{s}^{-1}$ . Special solderjoint specimens were manufactured [6]. Dog bone round cross-section specimens consist of two copper pieces between which 0.5mm of solder paste Sn-3.5Ag-0.75Cu was applied [6]. The number of cycles to failure was evaluated according to the criterion of the percentage drop in tensile force in relation to the level determined during the measurement. The percentage drop value is typically in range from 2% to 30% [8]. In our case, the crack initiation was determined as the number of cycles corresponding to a 20% force reaction drop of extrapolated force over the upper curve of tensile force vs. number of cycles. In the Fig. 1, the main results of the test evaluation are shown, whereas the number of cycles to failure was determined to 85. There is also presented the uniaxial hysteresis loop in half-life on the right side of the Fig.1.



Fig. 1: Evaluation of the crack initialization (left), half-life hysteresis loop (right)

These tension-compression fatigue tests were performed for four strain amplitude levels. Strain amplitudes from hysteresis loops in the half-life were used to construct the e-N curve (Fig. 2). The stiffness of cooper parts was taking into account in evaluations considering Hooke's law with elastic properties of copper (Young modulus E=137.6 GPa, Poisson ratio  $\nu=0.34$ ).



Fig. 2: Lifetime curve for Sn-3.5Ag-0.75Cu of tension-compression fatigue

The second study will presents the influence of mean stress and stress amplitude on the accumulation of axial strain in specimens. Uniaxial ratcheting was investigated for three different loading frequencies 0.25Hz, 0.35Hz and 0.5Hz. The test consisted of seven loading blocks. In the first three loading blocks with duration of 50 cycles per block, the force amplitude was incrementally increased while mean force value remained the same. In the following four loading blocks with duration of 25 cycles per block, the mean force value was step-wisely increased while force amplitude remained constant, see Table 1.

| Number of cycles per set | 50   | 50   | 50   | 25   | 25   | 25   | 25   |
|--------------------------|------|------|------|------|------|------|------|
| Force amplitude (N)      | 1500 | 1650 | 1800 | 1800 | 1800 | 1800 | 1800 |
| Mean force (N)           | 200  | 200  | 200  | 250  | 300  | 350  | 400  |

Table 1: Uniaxial ratcheting test conditions

The influence of stress amplitude on ratcheting in solderjoint was obtained from first three blocks in each test (Fig.3 left). The ratcheting strain is evaluated from measured elongation on 25 mm gauge length after subtracting elastic deformation of copper parts and considering the solderjoint thickness. From following blocks, the dependency of the mean stress on the ratcheting strain rate in solderjoint has been evaluated (Fig.3 right). The impact of mean stress as well as stress amplitude on ratcheting rate is almost linear in particular lower stress intervals.



Fig. 3: Dependency of the ratcheting strain rate on stress amplitude (left) and dependency of the ratcheting strain rate on mean stress (right)

### Viscoplastic model calibration

Data from described fatigue tests will be used to validate a viscoplastic material model using FE analysis. In this paper, we focused on the calibration of the non-unified material model [9] implemented into the ANSYS 2020R1 by a user-subroutine written in Fortran. AbdelKarim-Ohno kinematic hardening rule was also introduced in order to describe ratcheting behaviour properly. Basic constitutive model equations and material parameters optimized by analytical formulas based on experimental data from literature [3] are stated in Table 2 and Table 3 respectively. The results of predictions are shown in the Fig. 4. The advanced material model for capturing transient cyclic behaviour will be used also in a future study for simulations of fatigue tests presented here.



Fig. 4: Calibrated advanced material model considering monotonic tensile curves (left) and creep curves for Sn-3.5Ag-0.75Cu (experiment taken from [3])

$$\begin{split} \boldsymbol{\varepsilon} &= \boldsymbol{\varepsilon}^{\boldsymbol{e}} + \boldsymbol{\varepsilon}^{tr} + \boldsymbol{\varepsilon}^{ss}, \\ \boldsymbol{\sigma} &= \boldsymbol{D}^{\boldsymbol{e}} : \boldsymbol{\varepsilon}^{\boldsymbol{e}}, \\ \boldsymbol{\dot{\varepsilon}}^{tr} &= \frac{2}{3} \cdot g^{tr}(\overline{y}, p) \cdot \frac{s-a}{\overline{y}}, g^{tr} = A^{tr} \overline{y}^{m^{tr}}, \\ \boldsymbol{\dot{\varepsilon}}^{ss} &= \frac{2}{3} \cdot g^{ss}(\overline{s}) \cdot \frac{s}{\overline{s}}, g^{ss} = A^{ss} \overline{s}^{m^{ss}}, \\ \boldsymbol{a} &= \sum_{i=1}^{M} \boldsymbol{a}^{i}, \\ \boldsymbol{\dot{a}}^{i} &= \frac{2}{3} h^{i} \cdot \boldsymbol{\dot{\varepsilon}}^{tr} - \mu \cdot \boldsymbol{\dot{\xi}}^{i} \cdot \boldsymbol{a}^{i} \cdot \dot{p} - H(f^{i}) \cdot \boldsymbol{\dot{\xi}}^{i} \cdot \langle \boldsymbol{\dot{\lambda}}^{i} \rangle \cdot \boldsymbol{a}^{i}, \\ \boldsymbol{\dot{\lambda}}^{i} &= \boldsymbol{\dot{\varepsilon}}^{tr} : \frac{a^{i}}{h^{i}/\boldsymbol{\xi}^{i}} - \mu \dot{p}, f^{i} = \frac{3}{2} \boldsymbol{a}^{i} : \boldsymbol{a}^{i} - \left(\frac{h^{i}}{\boldsymbol{\xi}^{i}}\right)^{2}, \\ \overline{y} &= \sqrt{\frac{3}{2}} \|\boldsymbol{s} - \boldsymbol{a}\|, \ \overline{s} &= \sqrt{\frac{3}{2}} \|\boldsymbol{s}\|, \ p &= \sqrt{\frac{2}{3}} \|\boldsymbol{\dot{\varepsilon}}^{tr}\|, \end{split}$$

where  $\langle x \rangle$  means the Macaulay bracket ( $\langle x \rangle = (x + |x|)/2$ ),  $H(f^i)$  is the Heaviside step function and  $\varepsilon^e, \varepsilon^{tr}, \varepsilon^{ss}$ - elastic, transient and steady state strain tensors

- $\sigma$ , s stress tensor and its deviatoric part  $a, a^i$  - backstress and its *i*-th part  $D^e$ - material elastic stiffness 4<sup>th</sup> order tensor  $\overline{y}, \overline{s}$  - effective and equivalent stress p - accumulated plastic strain M – number of backstress parts
- Table 3: Material parameters obtained for Sn-3.5Ag-0.75Cu

$$\begin{split} & E = 29500 \text{MPa}, \ \nu = 0.35, \ A^{tr} = 7.2e - 9, \ m^{tr} = 4.1, \ A^{ss} = 5e - 25, \ m^{ss} = 12, \ \mu = 0.1 \\ & h^1 = 14000 MPa, \ \xi^1 = 2000, \ h^2 = 4000 MPa, \ \xi^2 = 1000, \ h^3 = 1800 MPa, \ \xi^3 = 600, \\ & h^4 = 675 MPa, \ \xi^4 = 450, \ h^5 = 500 MPa, \ \xi^5 = 250, \ h^6 = 375 MPa, \ \xi^6 = 125, \\ & h^7 = 200 MPa, \ \xi^7 = 50, \ h^8 = 20 MPa, \ \xi^8 = 20 \end{split}$$

# Conclusions

The experimental program of Sn-3.5Ag-0.75Cu solder paste has been briefly described. The low-cycle fatigue tests realized under strain control will serve as a basis for identification of appropriate fatigue criterion. The response of considered lead-free solder paste reveals ratcheting with steady state. The ratcheting tests show important relationship between ratcheting rate and mean stress as well as stress amplitude.

With regard to stress-strain behaviour observed in the experimental campaign the most powerful nonlinear kinematic hardening rule has been stated according to AbdelKarim-Ohno [10]. Separate flow rules have been introduced leading to a non-unified theory. Material parameters of the advanced viscoplastic model were identified using data from literature based on analytical relations. The calibrated material model will be used in future simulation of fatigue tests.

Based on stress-strain history from described fatigue tests the viscoplastic material model will be calibrated for elevated temperatures. The optimization task will be done using the optiSlang software [11] similarly as presented elsewhere for Anand's viscoplastic model [12].

#### Acknowledgement

This work was supported by The Ministry of Education, Youth and Sports from the Specific Research Project (SP2020/23) by The Technology Agency of the Czech Republic in the frame of the project TN01000024 National Competence Center-Cybernetics and Artificial Intelligence and the Grant Agency of the Czech Republic (GACR) project No. 19-03282S. The support of Continental Automotive Czech Republic company is also acknowledged.

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